PC11 Radicals Practice (DO NOT WRITE ON THIS PAPER)

Radicals is a math topic that has a connection with exponents. A fractional exponent can be rewritten as a radical. This year in Pre-Calculus 11 we will focus on simplifying radicals and working with radical equations. Next year you will learn more about graphing and transforming radical functions. Visit hunkim.com/11 for more BC Pre-Calculus 11 resources.

- Simplifying radicals
- Ordering a set of irrational numbers
- Performing operations with radicals
- Solving simple (one radical only) equations algebraically and graphically
- Identifying domain restrictions and extraneous roots of radical equations
- 1. Evaluate $\sqrt{25}$
- 2. Solve $x^2 = 25$
- 3. Write as a mixed radical:
 - a. $\sqrt{8}$
 - b. $\sqrt{1575}$
- 4. Write as an entire radical
 - a. $2\sqrt{3}$
 - b. $3\sqrt[3]{2}$
 - c. $-2\sqrt[3]{3}$
- 5. If possible, evaluate
 - a. $\sqrt{-9}$
 - **b.** $\sqrt[3]{-8}$
 - c. $\sqrt{4\ 000\ 000}$
 - d. $\sqrt{0.25}$
 - e. $\sqrt{\frac{4}{9}}$
- 6. Order from least to greatest: $\sqrt{9}$, $2\sqrt{3}$, $\sqrt{30}$, π
- 7. $f(x) = \sqrt{x}$
 - a. Sketch and label 3 points
 - b. Evaluate f(25)
- 8. $y = \sqrt{x-2} 3$
 - a. Sketch
 - b. Domain?
 - c. Range?
- 9. $y = \sqrt{x a} + b$. Given a, b > 0, describe the transformation.

- 10. $y = -2\sqrt{x+1}$
 - a. Sketch and describe the transformation
 - b. Domain?
 - c. Range?
- 11. $y = a\sqrt{x+b} + c$ Given a, b, c > 0 describe the transformation.
- 12. Find the domain of:
 - a. $\sqrt{3-5x}$
 - b. $\frac{\sqrt{1-2x}}{1-2x}$
 - $\mathbf{c.} \quad \frac{\sqrt{3x-2}}{x^2-2}$
 - d. $\frac{2\sqrt{x}}{2\sqrt{x}}$
 - e. $\frac{\sqrt{2+5x}}{3x^2+13x-16}$
- 13. Rationalize:
 - a. $\frac{1}{\sqrt{2}}$
 - b. $\frac{4}{\sqrt{8}}$
 - c. $\frac{9}{6-\sqrt{3}}$
 - d. $\frac{5}{5+\sqrt{5}}$
 - e. $\frac{1}{\sqrt[3]{3}}$
- 14. Simplify $\sqrt{8} + 3\sqrt{2}$
- 15. Simplify $\sqrt{8} \sqrt[3]{32} + 3\sqrt{2} + \sqrt[3]{4}$
- 16. Simplify $\frac{\sqrt{12}}{2}$
- 17. Simplify $\frac{-2+\sqrt{12}}{-2}$
- 18. $2\sqrt{3} \times 3\sqrt{2}$

19.
$$(5\sqrt{5})(2\sqrt{5})$$

20.
$$\sqrt{2} \cdot \sqrt{3} \cdot \sqrt{5}$$

21.
$$a^b \cdot \sqrt{d} \cdot a^c \cdot \sqrt{e}$$

22. Expand and simplify:

a.
$$2\sqrt{2}(\sqrt{4}-3\sqrt{2}+1)$$

b.
$$(2 - \sqrt{2})^2$$

c.
$$(\sqrt{3}-\sqrt{2})(\sqrt{3}+\sqrt{2})$$

d.
$$3(\sqrt{8}-\sqrt{2})(1-\sqrt{8})$$

e.
$$(\sqrt{8} - 1)^3$$

f.
$$(\sqrt{2} - \sqrt{3})(2 + \sqrt{6} + 3)$$

23. A rectangle has a base of $4\sqrt{2} - 2\sqrt{3}$

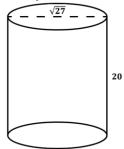
and a height of $\sqrt{8}-\sqrt{3}$

- a. Area in simplified form?
- b. Perimeter in simplified form?

24. A cylinder has a diameter of $\sqrt{8}$ and a height of 10

- a. Volume?
- b. Area including the bottom?

25. See cylinder below:



- a. Volume?
- b. Area including the bottom?

26. Solve:

a.
$$\sqrt{x} = 3$$

b.
$$2\sqrt{x} = 4$$

c. Solve
$$\sqrt{x-2}=3$$

27. $\sqrt{x+4} = 2 - x$

- a. Estimate the solution graphically
- b. Find the point of intersection algebraically
- c. Check for extraneous roots
- d. Find the point of intersection

28. Solve
$$\sqrt{x-1} = 2 - \frac{x}{2}$$

29. Solve
$$\sqrt{3x-2}-1=6-\frac{x}{2}$$

Challenge:

30. Enrichment: Solve
$$\sqrt{x+1} - 2 = \sqrt{x-3}$$

31. Enrichment:

- a. Define: |a|
- b. Simplify $\sqrt{x^2}$
- c. Simplify $\sqrt{x^4}$
- d. Simplify $\sqrt{x^6}$
- e. Simplify $\sqrt{a^2b^8c^{14}}$